

Commutative

$$A \cup B = B \cup A$$

$$A \cap B = B \cap A$$

Associative

$$A \cup (B \cup C) = A \cup (B \cup C)$$

$$A \cap (B \cap C) = A \cap (B \cap C)$$

Neutral element

$$A \cup \emptyset = A$$

$$A \cap E = A$$

Absorbing element

$$A \cup E = E$$

$$A \cap \emptyset = \emptyset$$

Distributive

$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$

De Morgan's laws

$$\overline{A \cap B} = \bar{A} \cup \bar{B}$$

$$\overline{A \cup B} = \bar{A} \cap \bar{B}$$

Laplace laws

$$P(A) = \frac{\text{Number of ways it can happen}}{\text{Total number of outcomes}}$$

Complement of an Event

$$P(\bar{A}) = 1 - P(A)$$

Union of Events

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

Conditional Probability

$$P(A | B) = \frac{P(A \cap B)}{P(B)}$$

Independent Events

$$P(A | B) = P(A)$$

$$P(A \cap B) = P(A) \times P(B)$$

Permutation

$$P_n = n! = n \times (n - 1) \times \dots \times 2 \times 1$$

$$\text{ex: } P_4 = 4! = 4 \times 3 \times 2 \times 1 = 24$$

Permutations without repetition

$${}^n A_p = \frac{n!}{(n - p)!}$$

$$\text{ex: } {}^6 A_2 = \frac{6!}{(6 - 2)!} = 30$$

Permutations with repetition

$${}^n A'_p = n^p$$

$$\text{ex: } {}^5 A'_3 = 5^3 = 125$$

Combination

$${}^n C_p = \frac{{}^n A_p}{p!} = \frac{n!}{(n - p)! \times p!}$$

$$\text{ex: } {}^5 C_4 = \frac{{}^5 A_4}{4!} = 5$$