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Complex number  $z = a + bi$

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Conjugate  $\bar{z} = a - bi$

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Symmetry  $-z = -a - bi$

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Equality  $a + bi = c + di \Leftrightarrow a = c \wedge b = d$

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Algebraic Form

Addition  $(a + bi) + (c + di) = (a + c) + (b + d)i$

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Subtraction  $(a + bi) - (c + di) = (a - c) + (b - d)i$

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Multiplication  $(a + bi) \times (c + di) = (ac - bd) + (ad + bc)i$

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Division  $\frac{a + bi}{c + di} = \frac{a + bi}{c + di} \times \frac{c - di}{c - di} = \frac{ac + bd}{c^2 + d^2} + \frac{bc - ad}{c^2 + d^2}i$

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Angle  $arg(z) = \theta$   $\theta = \tan^{-1}\left(\frac{b}{a}\right)$

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Trigonometric to Algebraic form conversion

Distance  $|z| = \rho$   $\rho = \sqrt{a^2 + b^2}$

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Complex number  $z = \rho \cdot cis(\theta)$   $z = \rho \cdot (\cos \theta + i \sin \theta)$

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Conjugate  $\bar{z} = |\rho| \cdot cis(-\theta)$

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Symmetry  $-z = |\rho| \cdot cis(\theta + \pi)$

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Trigonometric Form

Multiplication  $z_1 \times z_2 = \rho_1 \rho_2 \cdot cis(\theta_1 + \theta_2)$

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Division  $\frac{z_1}{z_2} = \frac{\rho_1}{\rho_2} \cdot cis(\theta_1 - \theta_2)$

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Inverse  $z^{-1} = \frac{1}{z}$   $z^{-1} = \frac{1}{\rho} \cdot cis(-\theta)$

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Exponentiation  $z^n = \rho^n \cdot cis(n\theta)$

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De Moivre's Formula

Radicals  $\sqrt[n]{\rho \cdot cis \theta} = \sqrt[n]{\rho} \cdot cis\left(\frac{\theta + 2k\pi}{n}\right), k \in \{0, \dots, n-1\}, n \in \mathbb{N}$