

Average rate of change between two points

Slope of the Secant Line $[a, b]$ $SSL = \frac{f(b) - f(a)}{b - a}$

Rate of change at a point

$$f'(x_0) = \lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0} \quad f'(x_0) = \lim_{h \rightarrow 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

Constant

$$a' = 0 \quad \text{ex: } 4' = 0$$

Multiplication by constant

$$(mx)' = m \quad \text{ex: } (3x)' = 3$$

Power Rule

$$(u^n)' = n \times u^{n-1} \times u' \quad \text{ex: } ((6x)^5)' = 5(6x)^4 \times (6x)' = 5(6x)^4 \times 6$$

Root

$$(\sqrt[n]{u})' = \frac{u'}{n \times \sqrt[n]{u^{n-1}}} \quad \text{ex: } (\sqrt{2x})' = \frac{(2x)'}{2 \times \sqrt{2x}} = \frac{1}{\sqrt{2x}}$$

Exponential

$$(a^u)' = u' \times a^u \times \ln a \quad \text{ex: } (7^{3x})' = 3 \times 7^{3x} \times \ln 7$$

Exponential base e

$$(e^u)' = u' \times e^u \quad \text{ex: } (e^{2x})' = 2 \times e^{2x}$$

Sum Rule

$$(u + v)' = u' + v' \quad \text{ex: } (2x + 5)' = (2x)' + 5' = 2$$

Product Rule

$$(u \times v)' = u'v + uv' \quad \text{ex: } (x^2 \times e^x)' = (x^2)'e^x + x^2(e^x)' = 2xe^x + x^2e^x$$

Quotient Rule

$$\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2} \quad \text{ex: } \left(\frac{x+1}{2x}\right)' = \frac{(x+1)' \times (2x) - (x+1) \times (2x)'}{(2x)^2}$$

Chain Rule

$$(g \circ f)' = g'(f) \times f' \quad \text{ex: } g(x) = 2x^2; g'(x) = 4x; f(x) = 2x; f'(x) = 2 \\ (g \circ f)' = 4(2x) \times 2$$

Sine

$$(\sin u)' = u' \times \cos u \quad \text{ex: } (\sin(6x))' = 6 \times \cos(6x)$$

Cosine

$$(\cos u)' = -u' \times \sin u \quad \text{ex: } (\cos(3x))' = -3 \times \sin(3x)$$

Tangent

$$(\tan u)' = \frac{u'}{\cos^2 u} \quad \text{ex: } (\tan(x))' = \frac{1}{\cos^2 x}$$

Logarithms

$$(\log_a u)' = \frac{u'}{u \times \ln a} \quad \text{ex: } (\log_4(6x))' = \frac{(6x)'}{6x \ln 4} = \frac{6}{6x \ln 4} = \frac{1}{x \ln 4}$$

Natural logarithm

$$(\ln u)' = \frac{u'}{u} \quad \text{ex: } (\ln(5x))' = \frac{(5x)'}{5x} = \frac{5}{5x} = \frac{1}{x}$$